Parallel Algorithm Construction

- Parallel algorithms for MIMD machines can be divided into 3 categories,
- \square these are :
 - Pipelined Algorithms / Algorithmic Parallelism
 - Partitioned Algorithms / Geometric Parallelism
 - Asynchronous / Relaxed Algorithms

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Pipelined Algorithms / Algorithmic Parallelism

- A pipelined algorithm is an ordered set of (possibly different) processes in which the output of each process is the input to its successor.
- □ The input to the first process is the input to the algorithm
- The output from the last process is the output of the algorithm.

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Pipelined Algorithms

- Typically each processor forms part of a pipeline and
- performs only a small part of the algorithm.
- Data then flows through the system (pipeline) being operated on by each processor in succession.

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Example Say it takes 3 steps A, B & C to assemble a widget and assume each step takes one unit of time. Sequential widget assembly machine: Spends 1 unit of time doing step A followed by 1 unit of time doing step B, followed by 1 unit of time doing step C. So a sequential widget assembler produces 1 widget in 3 time units, 2 in 6 time units etc. i.e. one widget every 3 units

Example

Pipelined widget assembly machine

- Say we use a 3 segment pipeline where each of the subtasks (A, B or C) is assigned to a segment
- i.e. the machine is split into 3 smaller machines; one to do step A, one for step B and one for step C and which can operate simultaneously.

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Example

- The first machine performs step A on a new widget every time step and
- passes the partially assembled widget to the second machine which performs step B.
- This is then passed onto the third machine to perform step C

Example

- This produces the first widget in 3 time units (as the sequential machine),
- but after this initial startup time one widget appears every time step.
- □ i.e. the second widget appears at time 4 the third widget appears at time 5 etc.

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Pipelined AlgorithmsT = 1, L = 100, n = 10⁶ then Tseq = 10⁸ and Tpipe = 100 + 10⁶ - 1 = 10⁶ + 99 Speedup = Tseq / Tpipe = 10⁸ / (10⁶ + 99) = 100 i.e. 100 fold increase in speed. In general as n tends to infinity speedup tends to L.

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Geometric Parallelism / Partitioned Algorithms

These algorithms arise when there is a natural way to decompose the data set into smaller "chunks" of

- which are then allocated to individual processors.
- Thus each processor contains more or less the same code but operates on a subset of the total data.

data,

Partitioned Algorithms

- The solution to these subproblems are then combined to form the complete solution.
- Depending on the algorithm being solved this combining of solutions usually implies
- communication synchronization among the processors.
- Synchronization means constraining a particular ordering of events.

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Partitioned Algorithms To illustrate the difference between pipelined and partitioned algorithms consider the following: Say an algorithm consists of 4 parts A, B, C and D and this algorithm is to operate on a data set E consisting of 4 subsets E1, E2, E3 and E4 (e.g. divide up matrix into submatrix)















Asynchronous / Relaxed Parallelism

- In relaxed algorithms there is no explicit dependency between processes,
- $\hfill\square$ as occurs in synchronized algorithms.
- □ Instead relaxed algorithms **never** wait for input.
- If they are ready they use the most recently available data



Example

Synchronous Operation

- □ A produces a1 passes it to B which calculates F1;
- □ A produces a2 passes it to B which calculates F2;
- □ i.e. B waits for A to finish (since B is faster than A) etc..

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Relaxed Parallelism

- □ Say we have 3 processors
- P1 : given x, P1 calculates F (x) in time t1, units and sends it to P3
- P2 :given y, P2 calculates F'(y) in time t2 units and sends it to P3
- P3 : given a, b, c, P3 calculates d = a b/c in time t3 units;
- □ if | d-a | > Epsilon then d is sent to P1 and P2 otherwise d is output.

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Example

Serial Mode

- P1 computes F(Xn)
- □ then P2 computes F'(Xn)
- then P3 computes Xn+1 using (1)
- So time per iteration is t1 + t2 + t3
- If k iterations are necessary for convergence then total time is k (t1 + t2 + t3)

Example

- Synchronous Parallel Mode.
 - P1 and P2 compute F(Xn) and F'(Xn) simultaneously and
 when BOTH have finished the values F(Xn) and F'(Xn) are used by P3 to compute Xn+1
 - Time per iteration is max(t1, t2) + t3

Again k iterations will be necessary so total time is k [max(t1,t2) + t3]

X1 = X0 - F(X0)/F'(X0) ...etc

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